

10.2 Calculus with Parametric Curves

單選題

1. Find the equation of the tangent to the curve $x = \cos t + \cos 2t$, $y = \sin t + \sin 2t$, at $t = \frac{\pi}{2}$.

(A) $y = 2x + 3$; (B) $y = 2x - 1$;
(C) $y = -2x - 1$; (D) $y = -2x + 3$.

Ans: A [102 學年度]

2. The area enclosed by the curve $x(t) = 1 + e^t$, $y(t) = t - t^2$ and the x -axis is
(A) $3 + e$; (B) $e - 1$; (C) $3 - e$; (D) $e - 2$.

Ans: C [104 學年度]

3. The **length** of the curve $x(t) = e^t \cos(t)$, $y(t) = e^t \sin(t)$, $0 \leq t \leq 1$, is
(A) $(e - 1)$; (B) $\sqrt{2}(e - 1)$; (C) e^π ; (D) $\sqrt{2}e^\pi$.

Ans: B [104 學年度]

4. Find the surface area generated by rotating the parametric curve C about the x -axis, where C is

$$\begin{cases} x = e^t - t, \\ y = 4e^{\frac{t}{2}}, \end{cases} \quad 0 \leq t \leq 2.$$

(A) $16\pi(\frac{1}{3}e^3 + e - \frac{4}{3})$; (B) $8\pi(\frac{1}{3}e^3 + e - \frac{4}{3})$;
(C) $2\pi(e^4 - 9)$; (D) $\pi(e^4 - 9)$.

Ans: A [102 學年度]

5. The **tangent** to the astroid $x(t) = 2 \cos^3(t)$, $y(t) = 2 \sin^3(t)$ at $t = \pi/4$ is

(A) $y = -x + \frac{\sqrt{2}}{2}$; (B) $y = -x + \sqrt{2}$; (C) $y = x + \frac{\sqrt{2}}{2}$; (D) $y = x + \sqrt{2}$.

Ans: B [103 學年度]

填充題

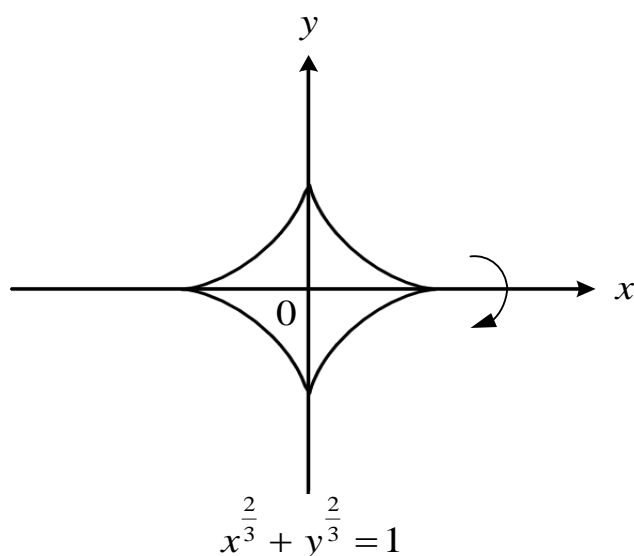
1. The **tangent line** equation of the parametric equation $x = \cos \theta + \sin 2\theta$,
 $y = \sin \theta + \cos 2\theta$ at the point when $\theta = 0$ in the Cartesian coordinate system is

_____ .

Ans: $y - 1 = \frac{1}{2}(x - 1)$ or $y = \frac{1}{2}x + \frac{1}{2}$ [100 學年度]

2. [100] Find the **area** of the surface obtained by rotating the curve $x^{\frac{2}{3}} + y^{\frac{2}{3}} = 1$

(parametrized by $x = \cos^3 \theta, y = \sin^3 \theta$) about the x -axis. _____



Ans: $\frac{12}{5}\pi$ [100 學年度]

3. The equation of the **tangent** to the curve $\begin{cases} x(t) = e^{\sqrt{t}} \\ y(t) = t - \ln(t^2) \end{cases}$ through the point
 $(x(1), y(1))$ is _____.

Ans: $y - 1 = -\frac{2}{e}(x - e)$ or $\frac{2}{e}x + y - 3 = 0$ [104 學年度]

4. The length of the parametric curve C :

$$\begin{cases} x = \cos t + t \sin t, \\ y = \sin t - t \cos t, \end{cases}$$

from $t = 0$ to $t = \pi$ is _____.

Ans: $\frac{\pi^2}{2}$ [101 學年度]